



2009 ESSS South American ANSYS Users Conference

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Test cases for variable density flow

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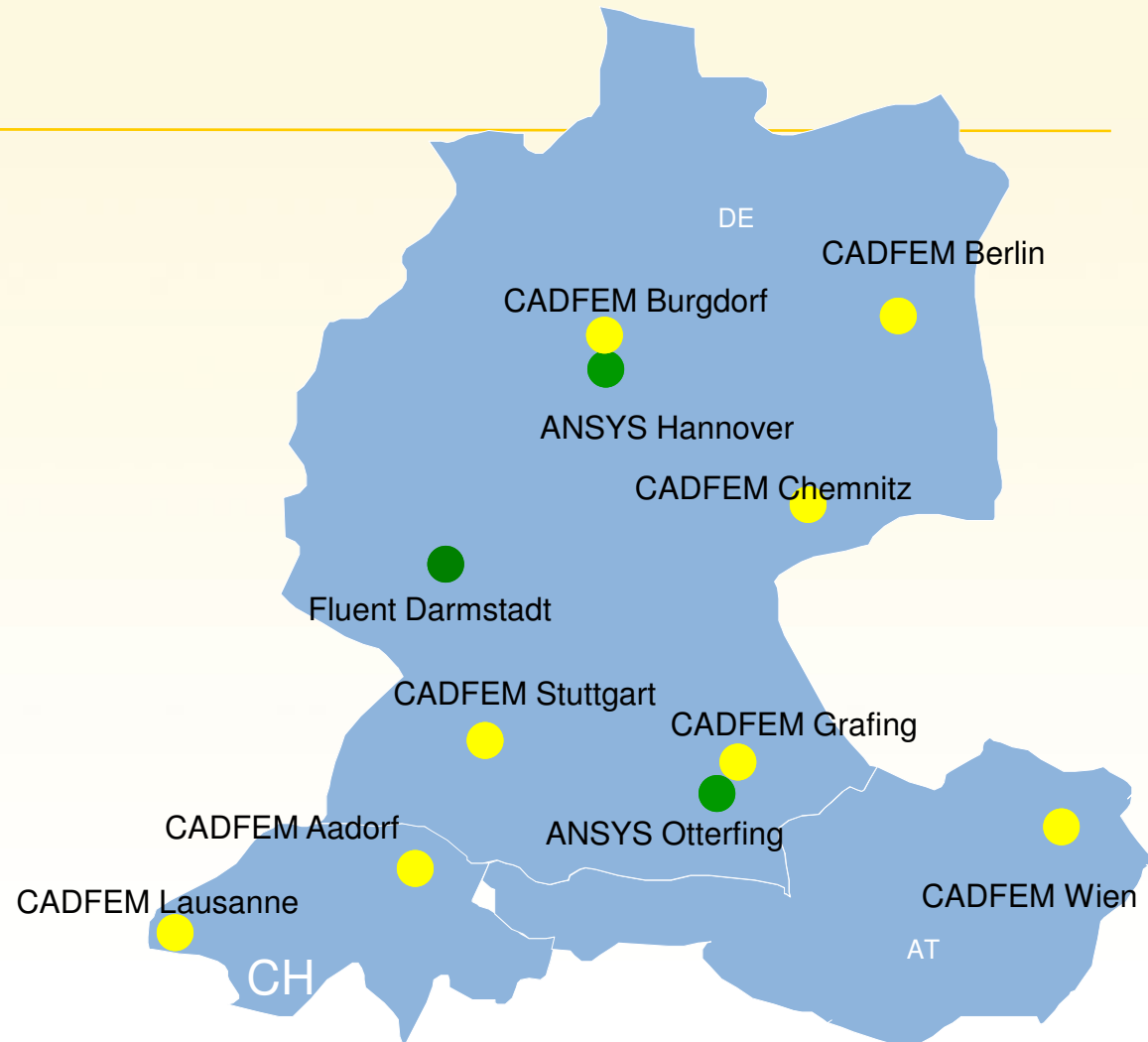
ANSYS Team Germany

CADFEM

- > 110 collaborators
- Established 1985
- Focus in FEM

ANSYS Germany

- > 114 collaborators
- Established 1990
- Focus in CFD





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Motivation

- Variable density flow modeling is challenging and not well understood
- Important for many industrial flows:
 - Reactor Safety
 - Chimney Plumes
 - Internal Combustion Engines
 - High Mach Number Flows
- To better understand the effects of variable density on flows, simple test cases were selected in order to test several aspects of these flows individually



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Test cases

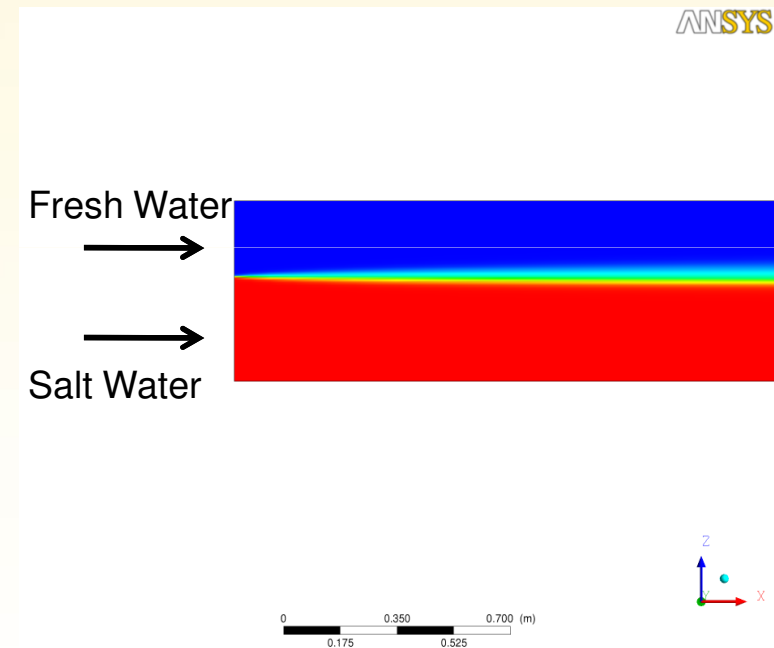
- In this presentation:
 - Saline Mixing Layer: different density fluids
 - Differenced Heated Cavity: density variation due to heating
- The densities differences involved in both test cases are not large
- In both test cases the flow has large buoyant effects



Saline Mixing Layer

- Fluids:
 - Fresh water: $\rho_1 = 1015 \text{ [kg/m}^3\text{]}$
 - Salt water: $\rho_2 = 1030 \text{ [kg/m}^3\text{]}$
 - Mixture Kinematic Diffusivity: $1\text{e-}9 \text{ [m}^2\text{/s]}$
- Inlet average velocities:
 - Fresh water inlet: $U_1 = 0.52 \text{ [m/s]}$
 - Salt water inlet: $U_2 = 0.32 \text{ [m/s]}$

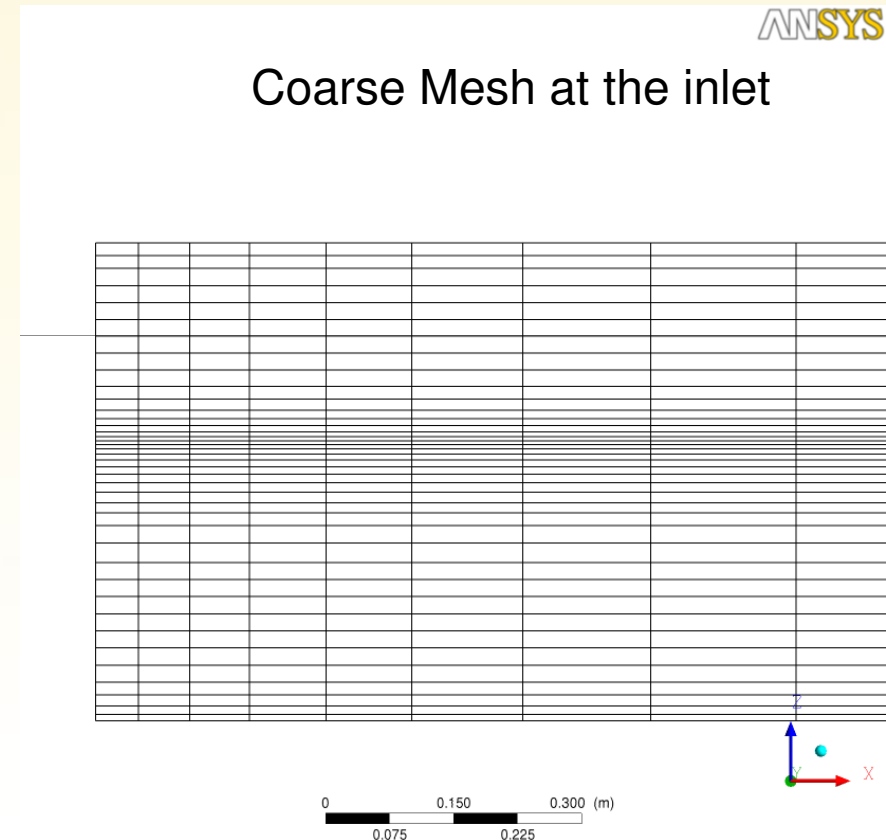
Experiment made by Uittenbogaard [1995]





Mesh

- Coarse Mesh (Grid01):
 - Mesh suggested by Uittenbogaard [1989]
 - 8160 hexahedral elements
- Fine mesh (Grid02):
 - Refined by a factor of 2 in each direction from Grid01
 - 32640 hexahedral elements





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Numerical Model

- CFX 12.0 version used for simulations
- 2D Flow
- Stationary Simulation
- High Resolution advection scheme
- First order turbulence Numeric's
- Automatic Time step (0.3 seconds on both meshes)
- Full Buoyancy model
- Convergence Criteria:
 - $1e-5$ RMS residuals



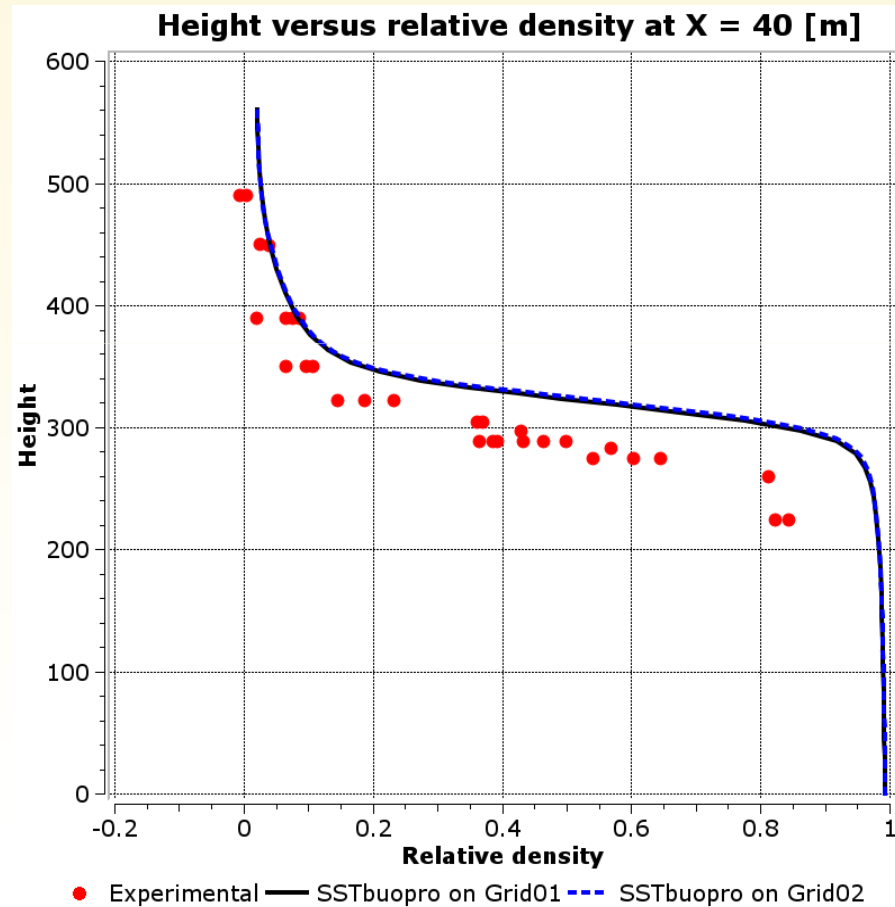
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Numerical Model

- Turbulence Models
 - SST
 - SST with buoyancy production for k (SSTbuopro)
 - K-Epsilon
 - K-Epsilon with buoyancy production for k (KEpsbuopro)



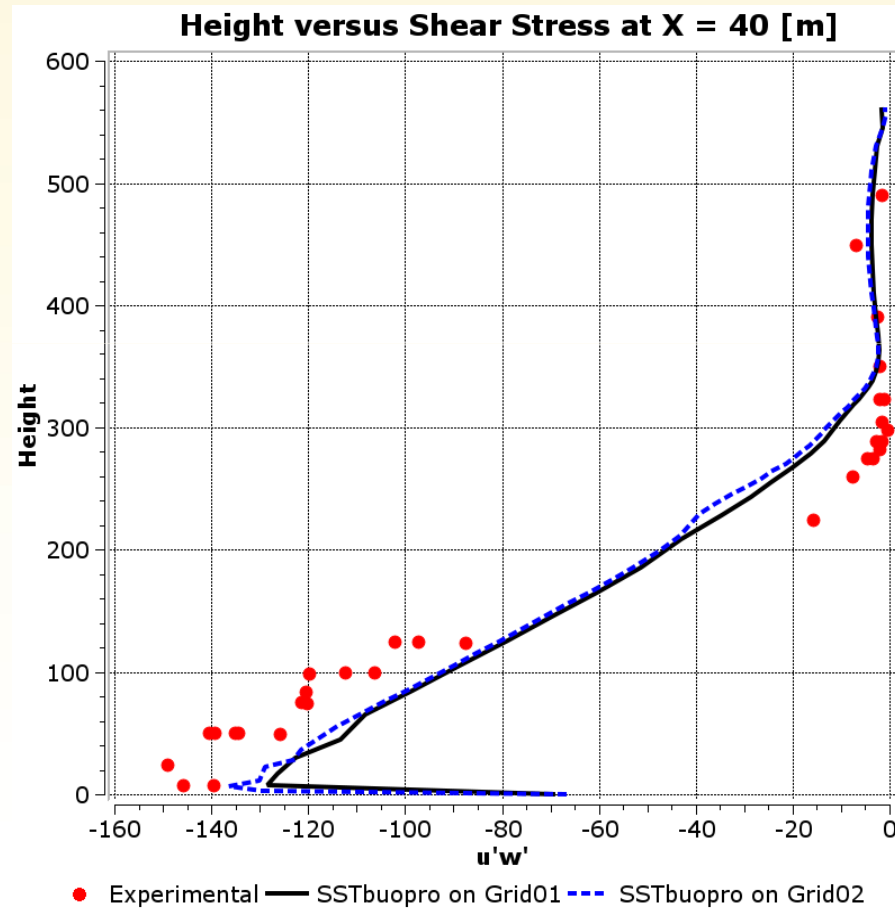
Mesh comparison



$$\rho_{rel} = \frac{\rho - \rho_{fresh}}{\rho_{salt} - \rho_{fresh}}$$



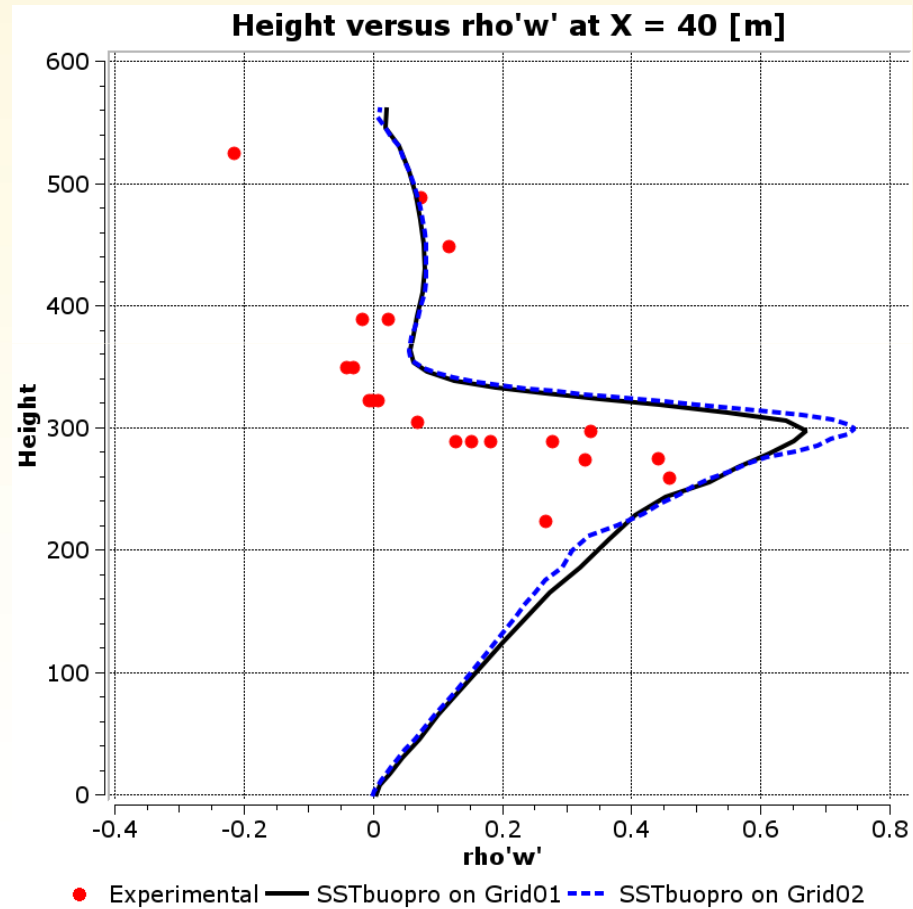
Mesh comparison



$$u'w' = -\left(\frac{\mu_t}{\rho}\right)\left(\frac{\partial w}{\partial x} + \frac{\partial u}{\partial z}\right)$$



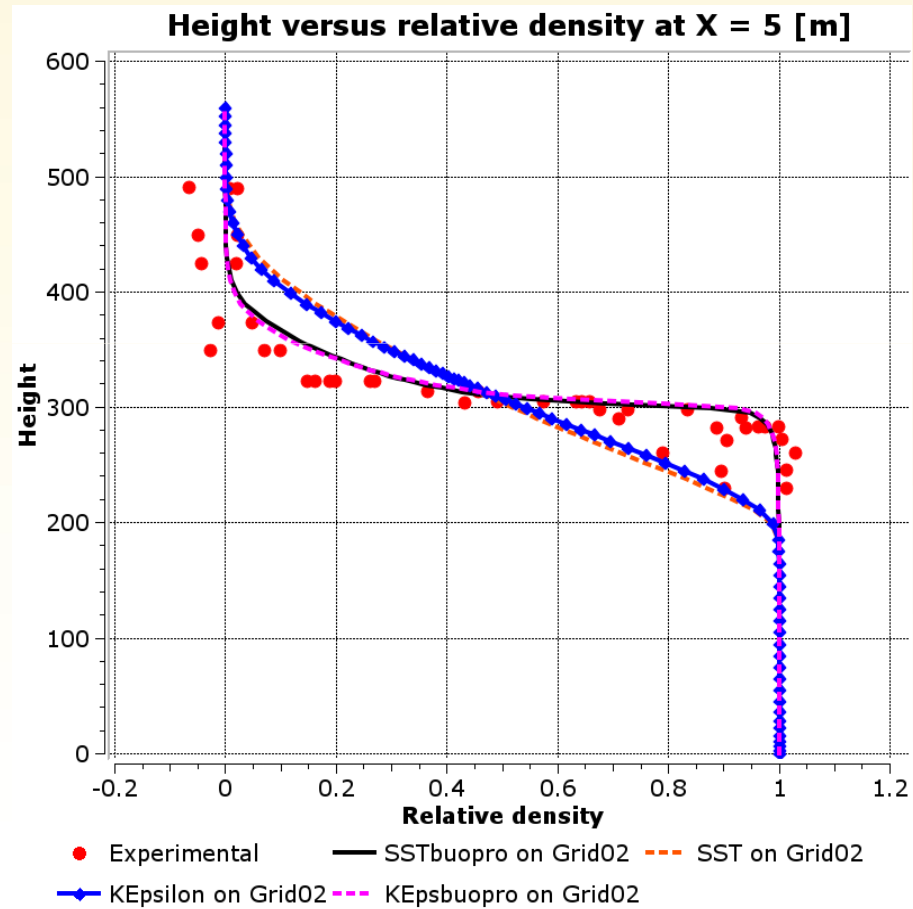
Mesh comparison



$$\rho'w' = -\left(\frac{\mu_t}{\rho.Sch}\right)\left(\frac{\partial\rho}{\partial z}\right)$$



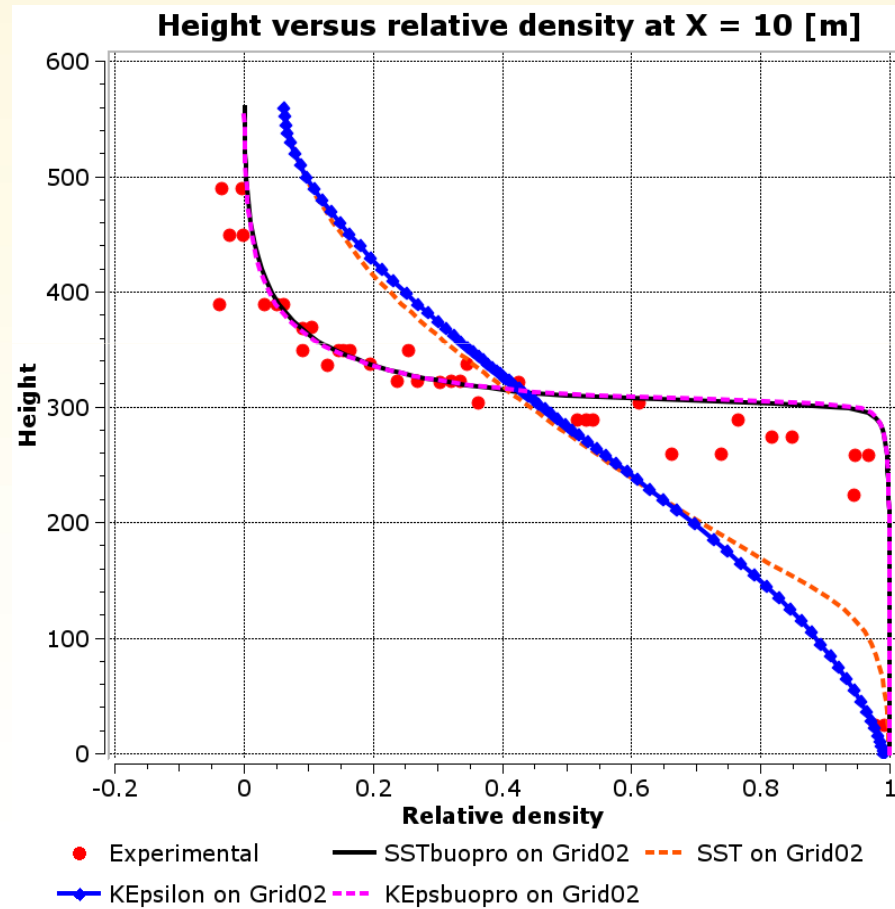
Model comparison



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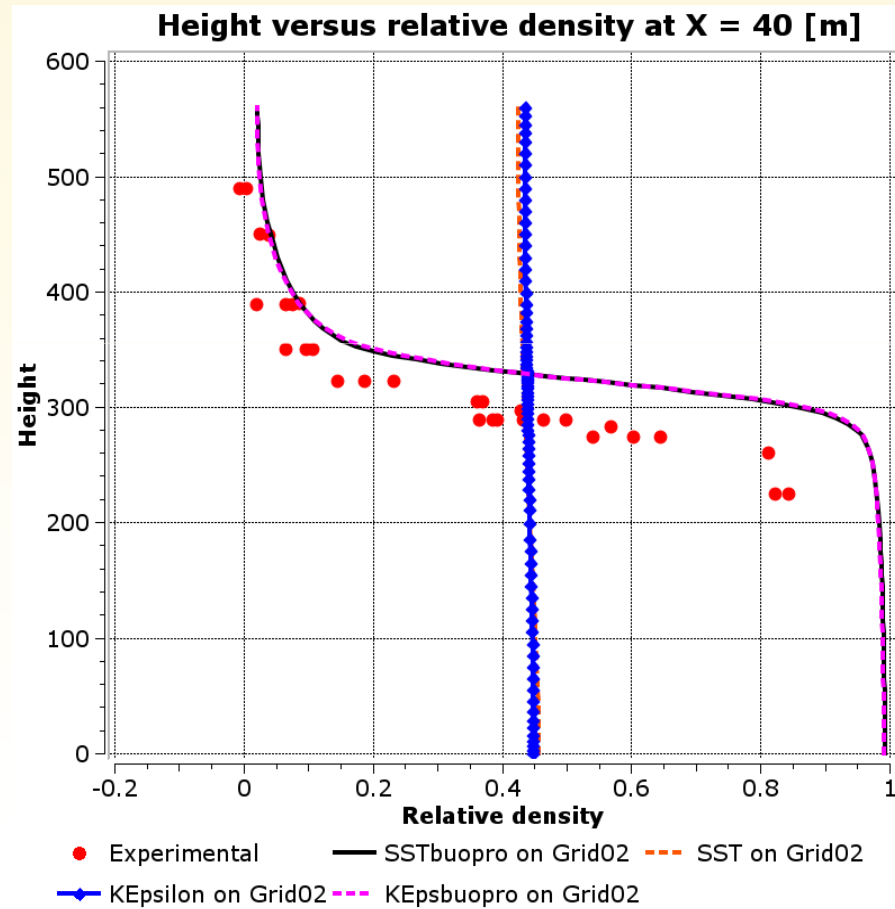
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Model comparison



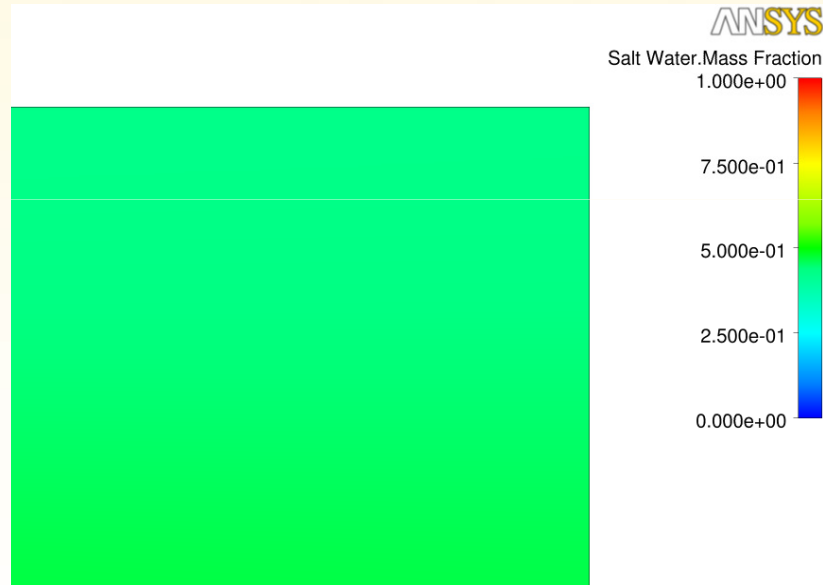
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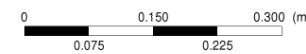
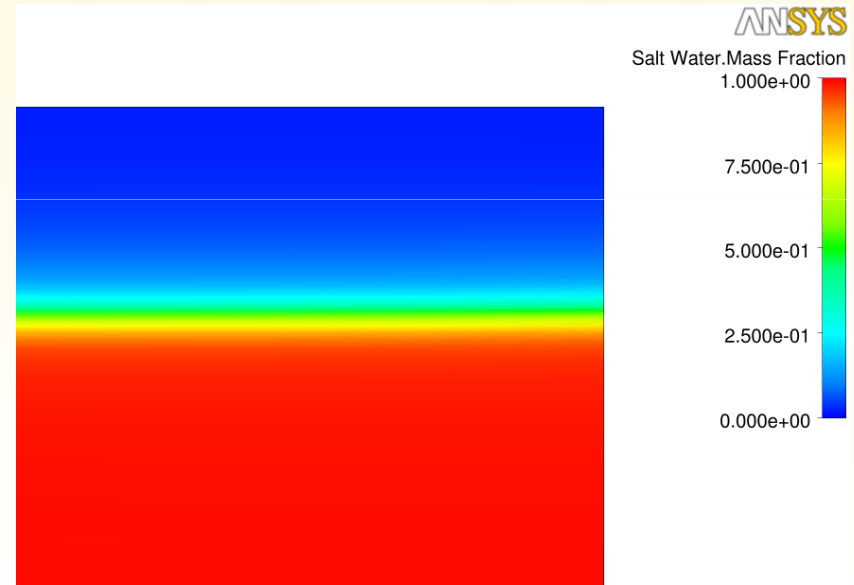
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Model Comparison - Salt Water Mass Fraction at the outlet

SST



SST with Buoyancy production for the k equation

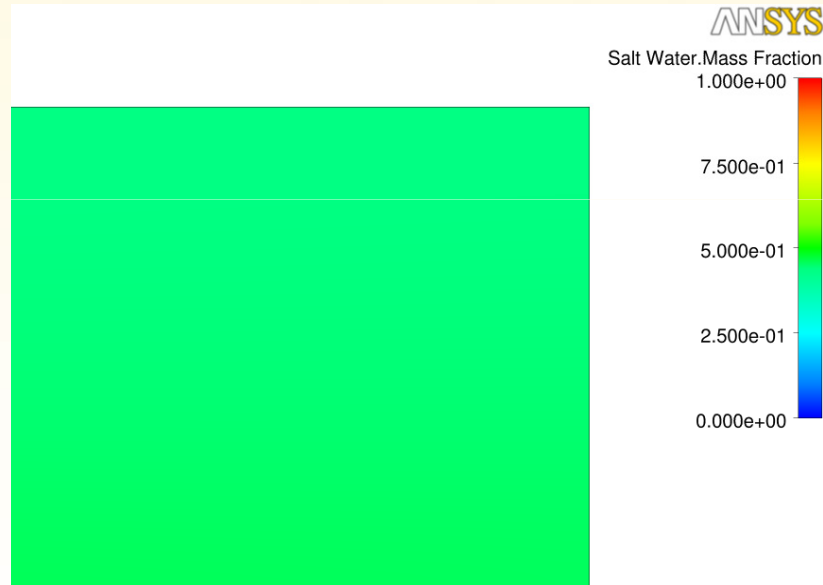




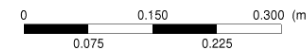
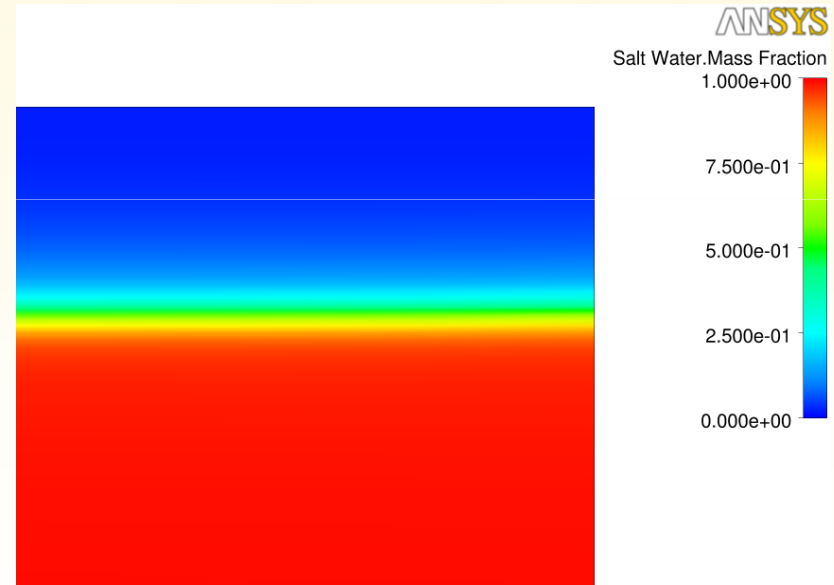
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Model Comparison - Salt Water Mass Fraction at the outlet

K Epsilon

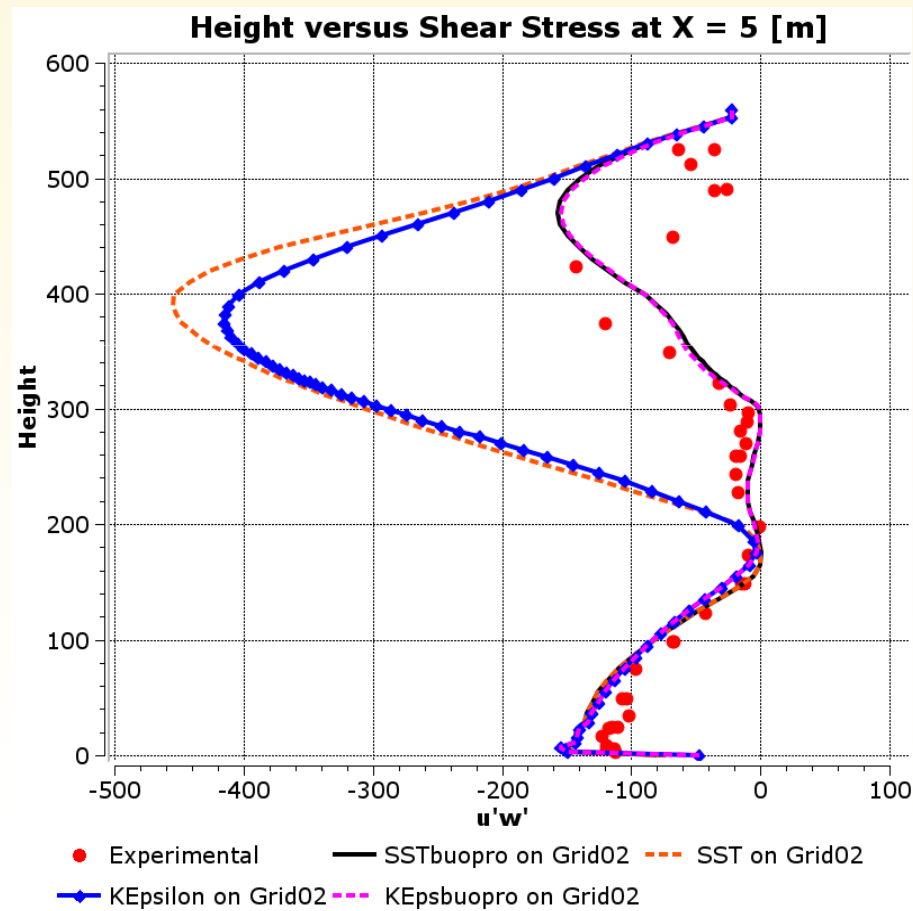


K Epsilon with Buoyancy production for the k equation





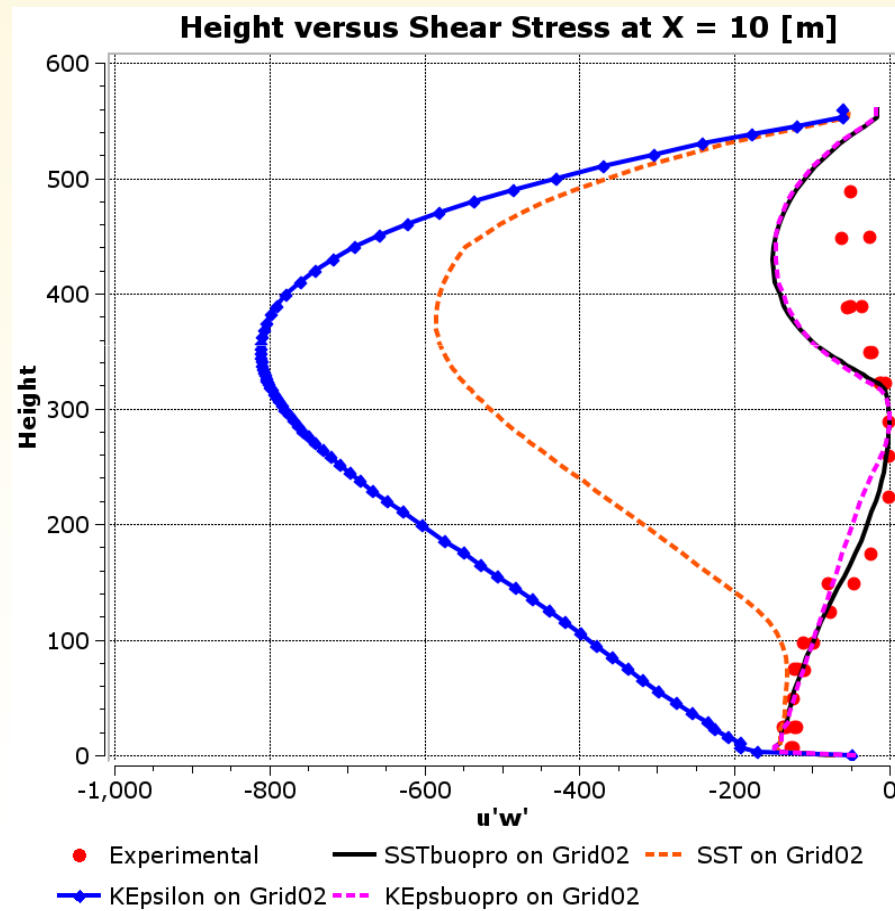
Model comparison



$$u'w' = -\left(\frac{\mu_t}{\rho}\right)\left(\frac{\partial w}{\partial x} + \frac{\partial u}{\partial z}\right)$$



Model comparison

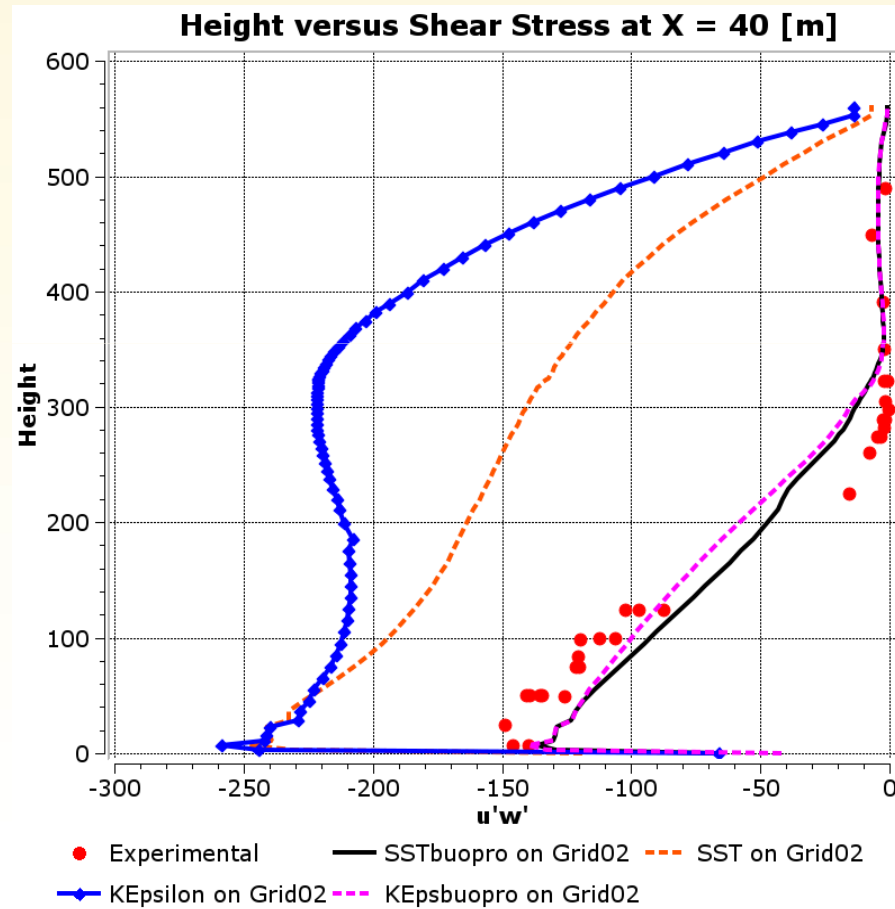


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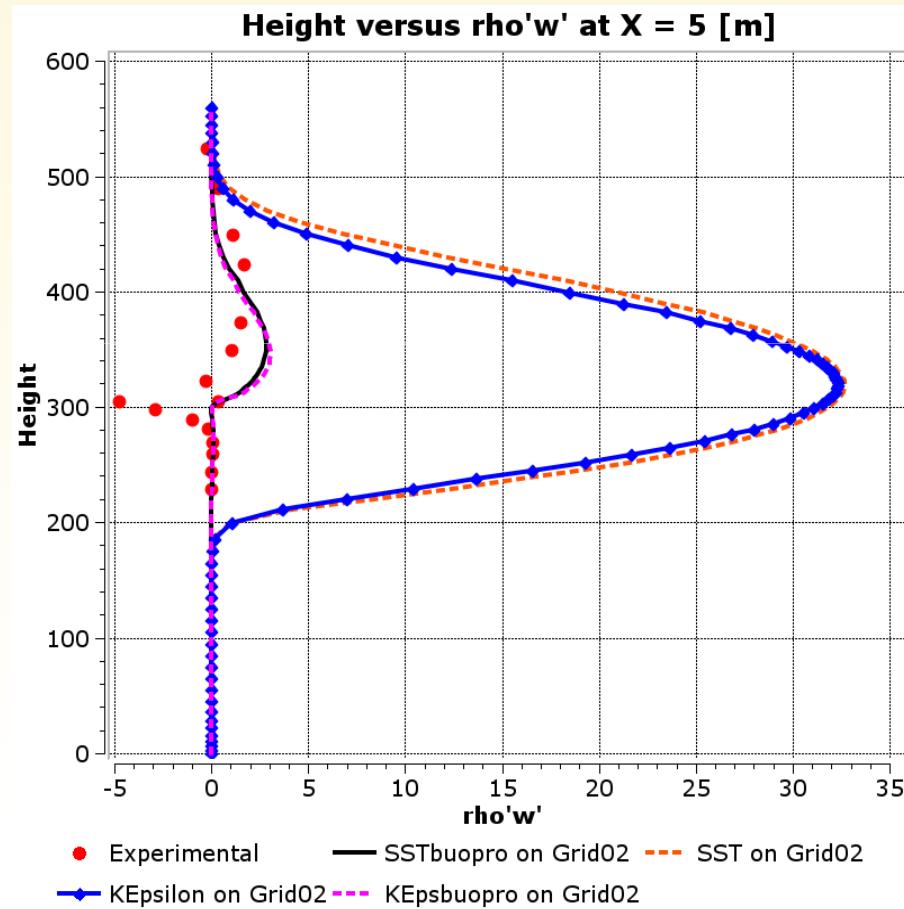
Model comparison



$$u'w' = -\left(\frac{\mu_t}{\rho}\right)\left(\frac{\partial w}{\partial x} + \frac{\partial u}{\partial z}\right)$$



Model comparison

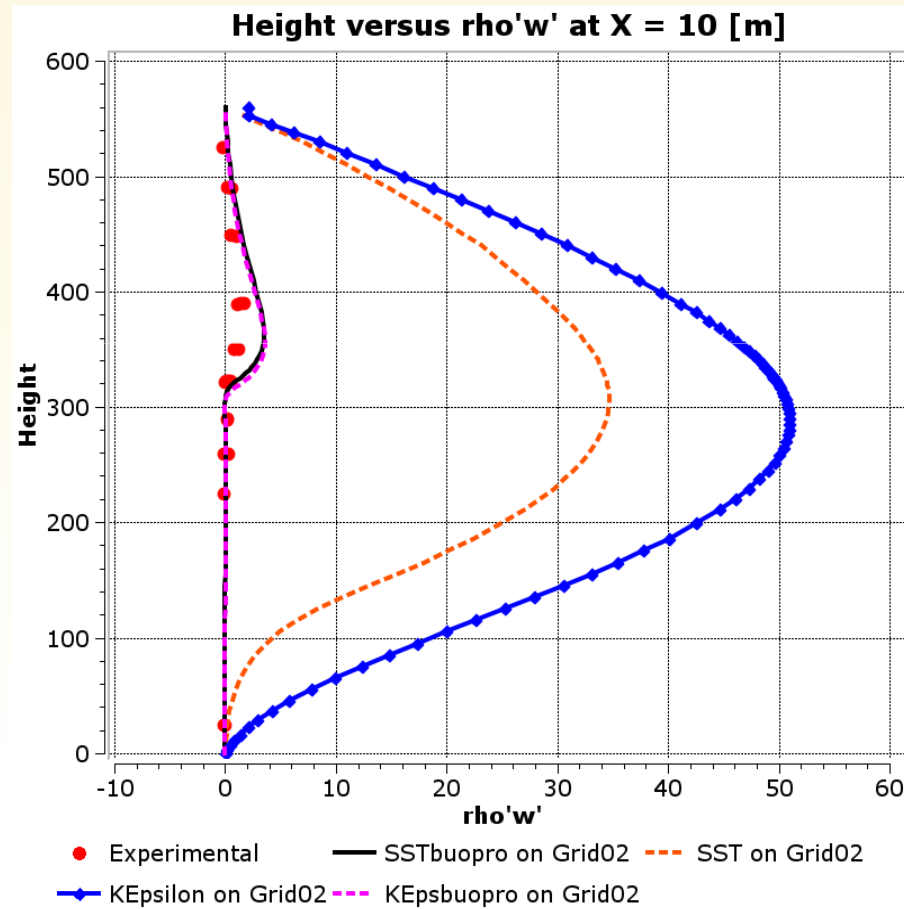


$$\rho'w' = - \left(\frac{\mu_t}{\rho.Sch} \right) \left(\frac{\partial \rho}{\partial z} \right)$$



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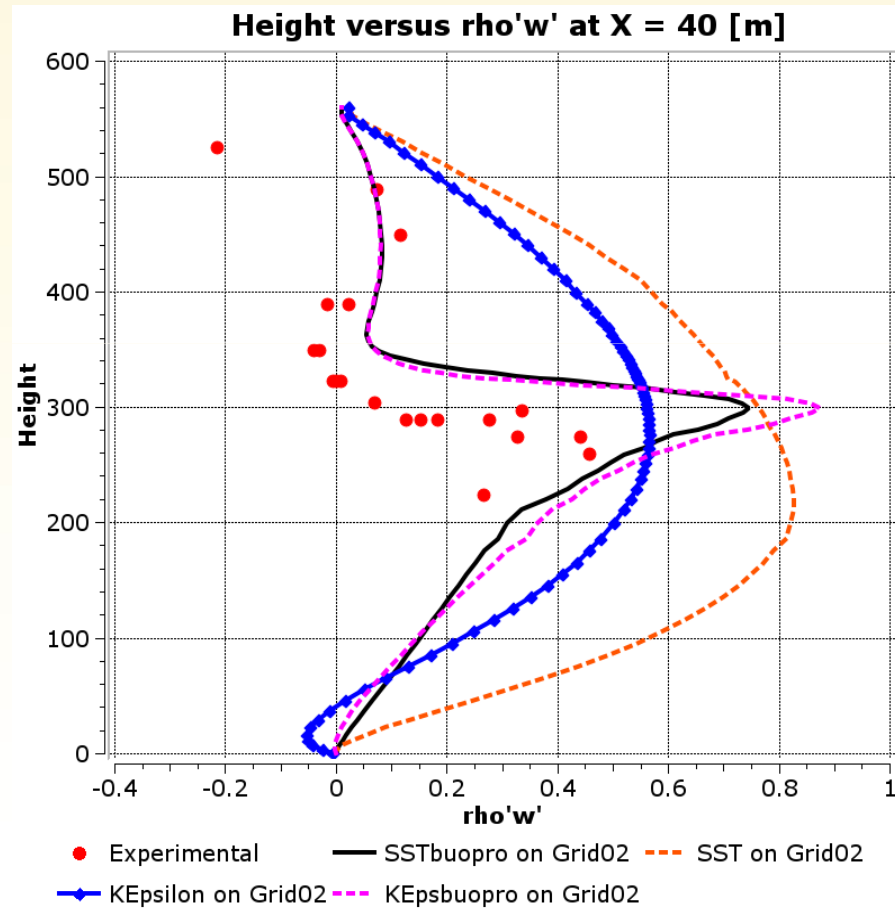
Model comparison



$$\rho'w' = -\left(\frac{\mu_t}{\rho.Sch}\right)\left(\frac{\partial\rho}{\partial z}\right)$$



Model comparison



$$\rho'w' = -\left(\frac{\mu_t}{\rho.Sch}\right)\left(\frac{\partial\rho}{\partial z}\right)$$



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Conclusions

- Mesh convergence was achieved (curves overlap)
- It is necessary to switch buoyancy turbulence on to match experimental results
- In the measurements made at 40 m from the inlet, the experimental values might be shifted because the experiment was conducted in an open channel leading to an inconstant free surface height



Description

- Experiment made by Cheesewright et al [1986]
- Cavity containing air

- Equation of state:
$$\rho = \frac{\rho_{ref} \cdot T_{ref}}{T}$$

- $T_{hot} = T_{Ref} + 0.5 \Delta T = 74.4 [^{\circ}C]$

- $T_{cold} = T_{Ref} - 0.5 \Delta T = 28.6 [^{\circ}C]$

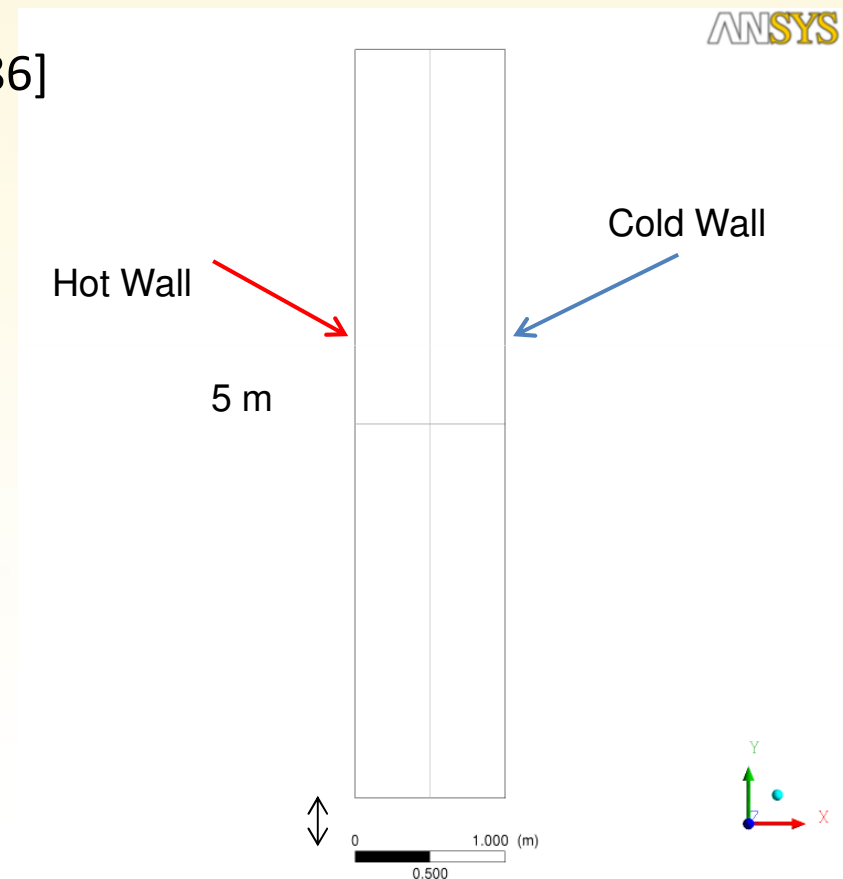
Where:

- $T_{ref} = 51.5 [^{\circ}C]$

- $\Delta T = 45.8 [^{\circ}C]$

- $P_{ref} = 1 [atm]$

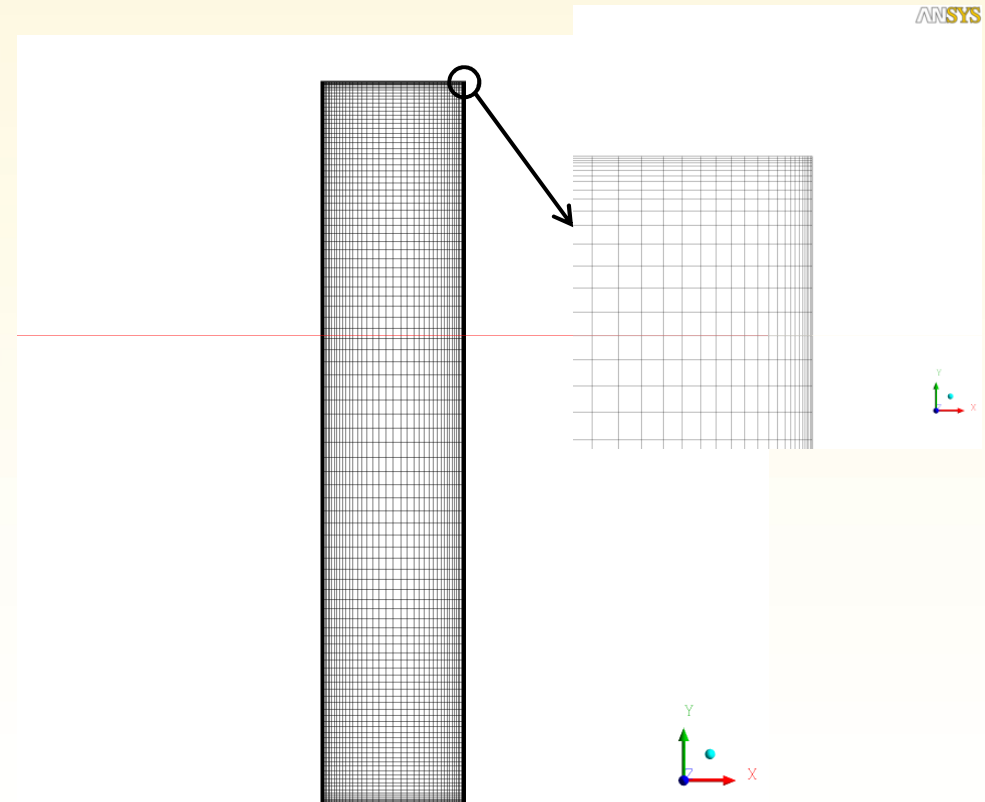
- $$\rho_{ref} = \frac{P_{ref} \cdot M}{T_{ref} \cdot R}$$





Mesh

- 2D Meshes
- Coarse Mesh:
 - 6272 hexahedral elements
 - $y^+=1.11$ with BSL model*
- Refined Mesh:
 - 25088 hexahedral elements
 - $y^+=1.18$ with BSL model*



*Average y^+ values

Coarse Mesh figures



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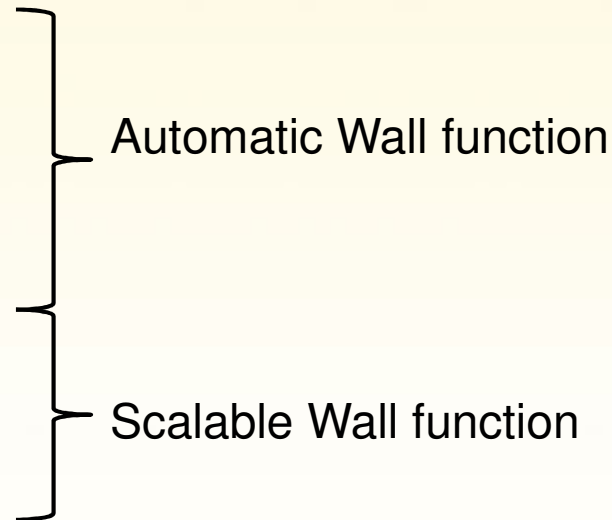
Numerical Model

- CFX 12.0 version used for simulations
- Stationary Simulation
- High Resolution advection scheme
- First order turbulence Numeric's
- Full Buoyancy Model
- Convergence Criteria:
 - $1e-5$ MAX residuals
 - $1e-5$ conservation target for the energy equation
 - 0.01 conservation target for other equations



Numerical Model

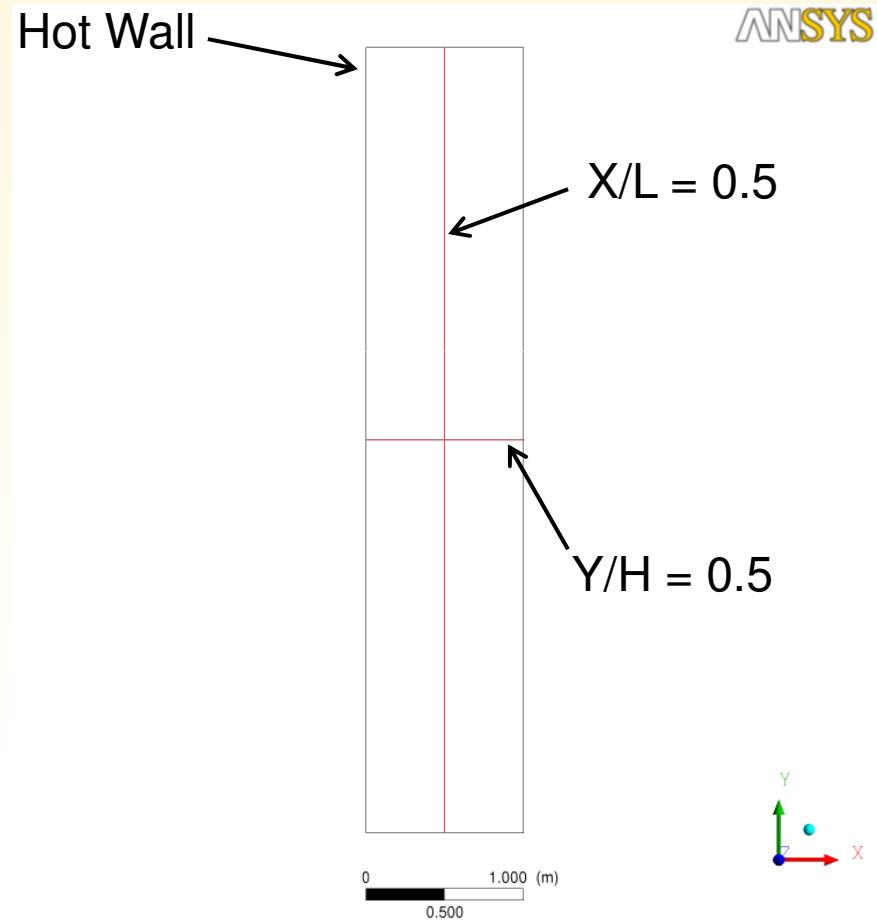
- Turbulence:
 - BSL
 - K – Omega
 - Reynolds Stress BSL
 - K – Epsilon
 - Reynolds Stress SSG
- Stationary simulation
- Pseudo time step:
 - Automatic time step (0.7 seconds for both meshes)





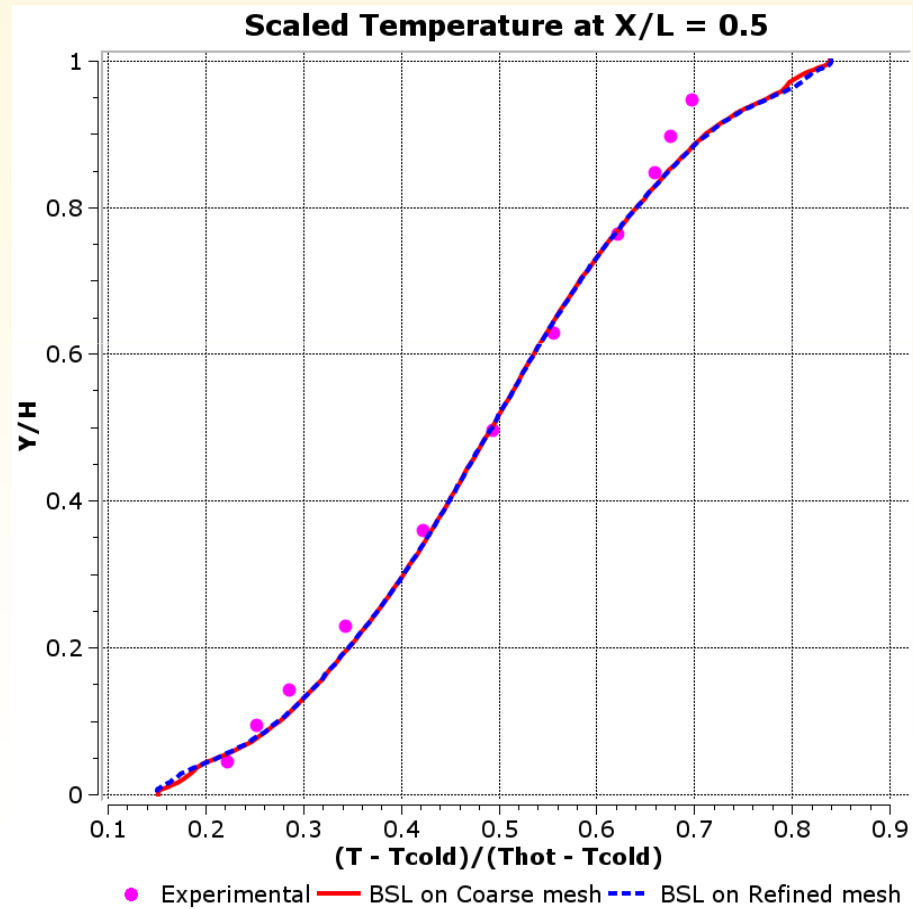
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Profiles Locations



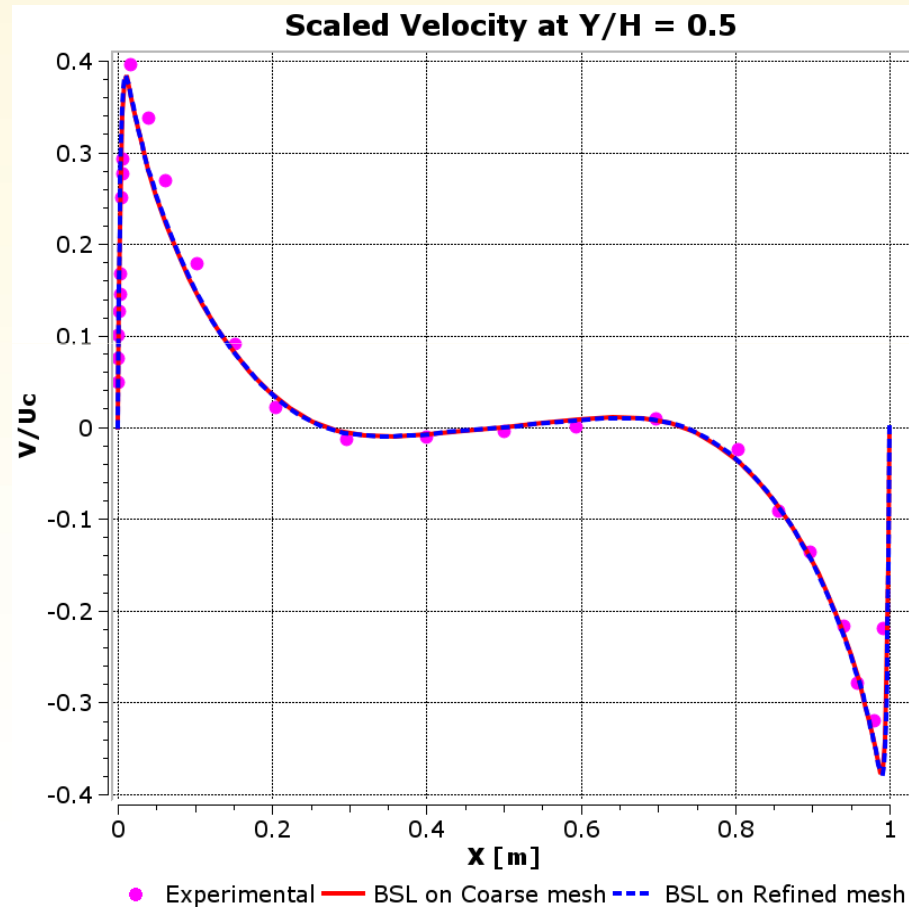


Mesh Comparison





Mesh Comparison



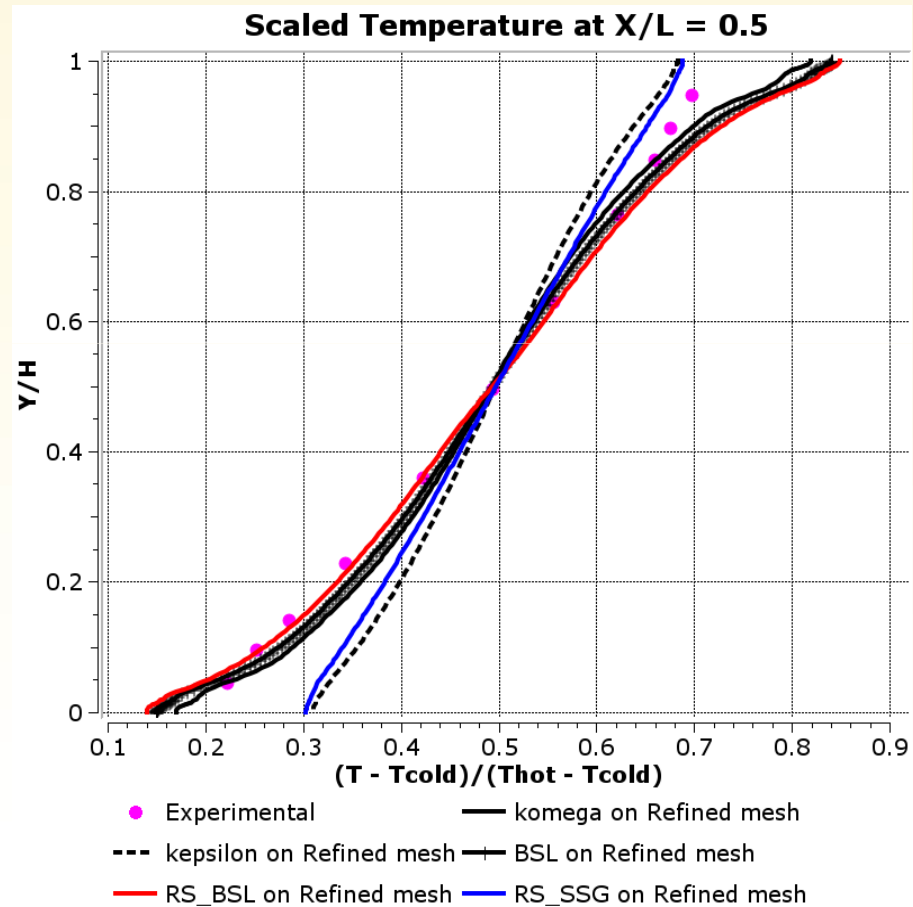
Where U_c is the convection velocity calculated as:

$$U_c = \sqrt{g \cdot \text{Width} \cdot \beta \cdot \Delta T}$$

Where β is the thermal expansion coefficient

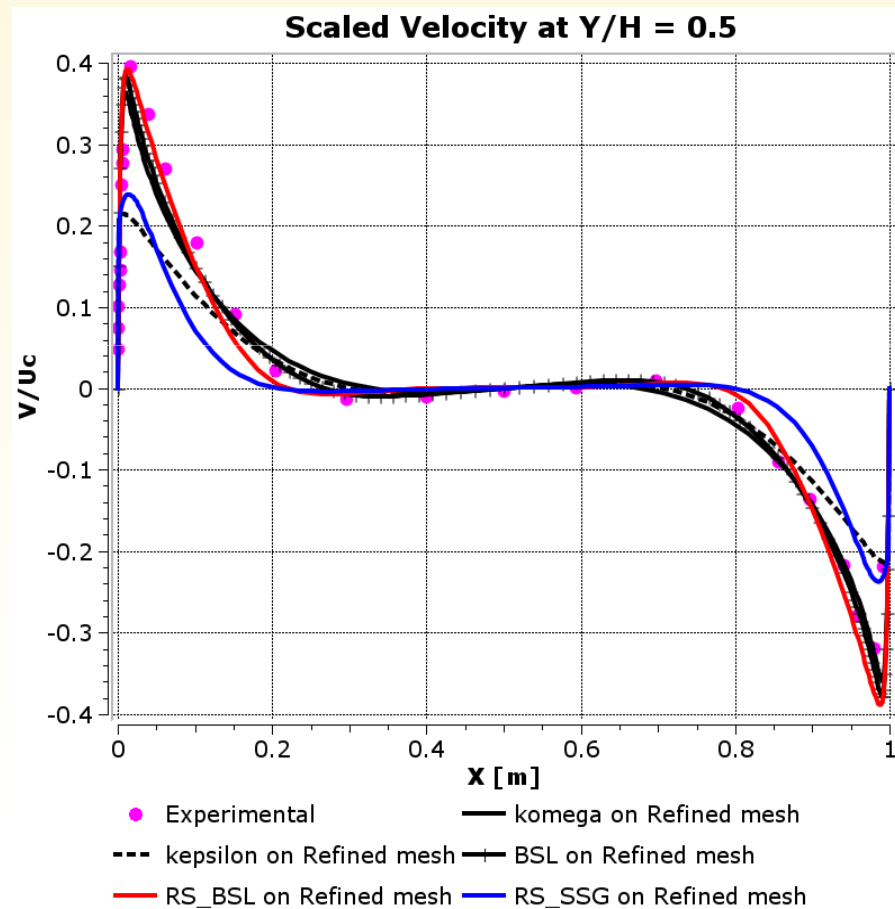


Model Comparison





Model Comparison



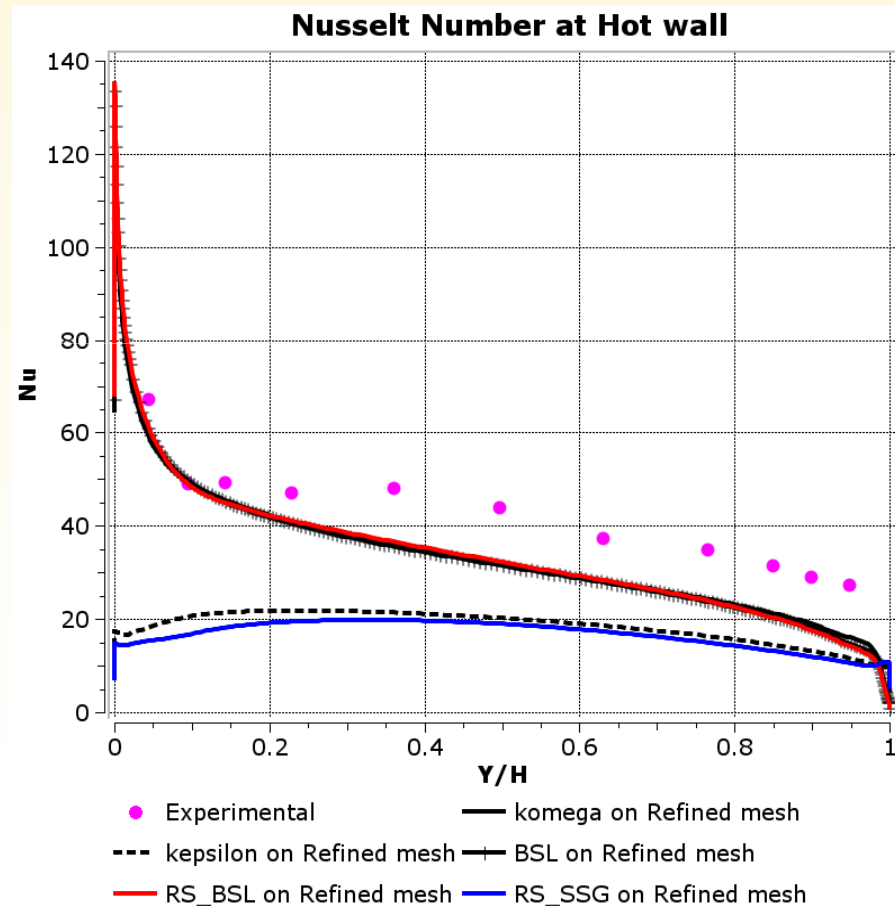
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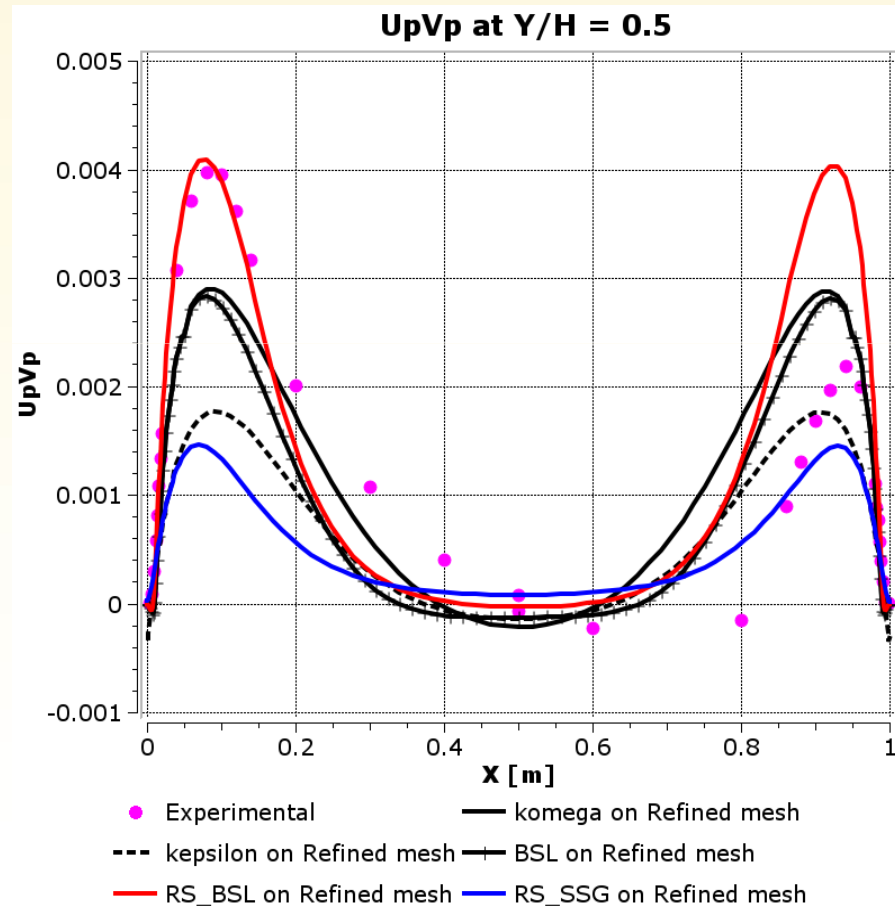


Model Comparison





Model Comparison

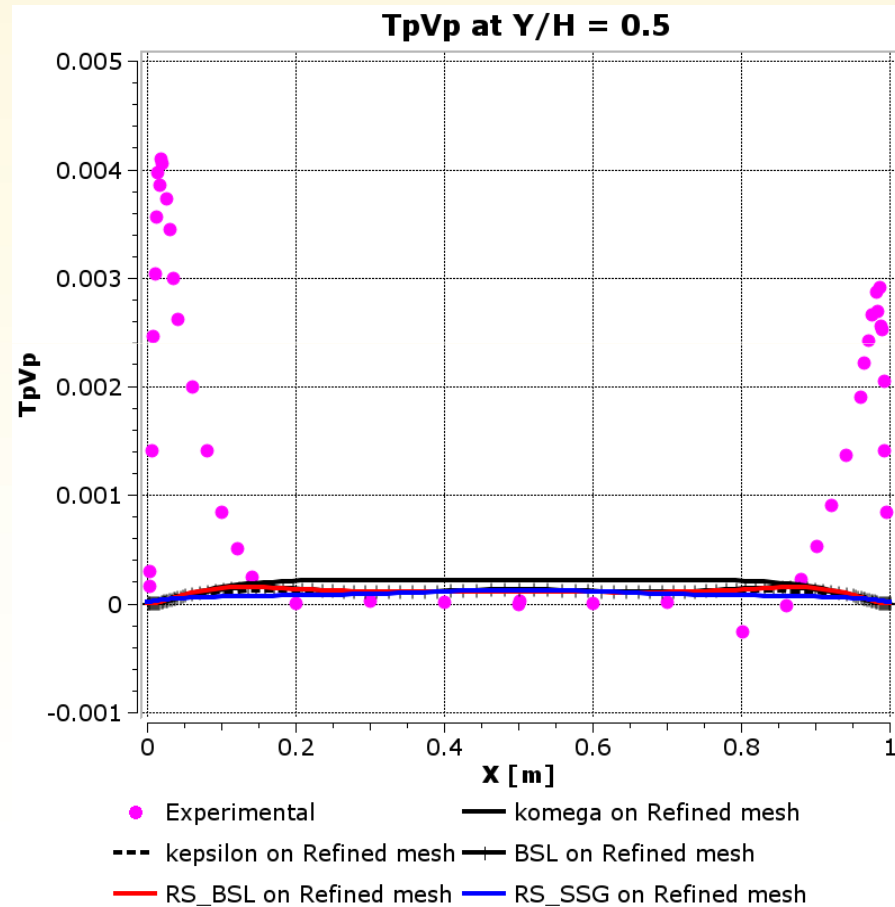


For the two equation models:

$$u'v' = - \frac{\left(\frac{\mu_t}{\rho} \right) \left(\frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right)}{U_c^2}$$



Model Comparison



$$T'v' = - \frac{\left(\frac{\mu_t}{\rho} \right) \left(\frac{\partial h}{\partial y} \right)}{0,9 \cdot \Delta T \cdot U_c \cdot c_p^{ref}}$$

Where:

$c_p^{ref} = 1.005 \text{ J Kg}^{-1} \text{ K}^{-1}$
 $h = \text{Static Enthalpy}$



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Conclusions

- Mesh convergence was achieved
- Omega based models in CFX resolve viscous sub-layer and therefore provide better prediction of the flow
- Omega based models correctly predict Nusselt numbers (turbulent heat flux normal to wall is correctly predicted)
- For all models the turbulent heat flux in the Y direction ($TpVp$) is greatly under predicted due to the turbulent Prandtl number approximation



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References

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- Uittenbogaard, R.E. [1995] The Importance of Internal Waves for Mixing in a Stratified Estuarine Tidal Flow
- R.Cheesewright, K.J.King and S.Ziai [1986] Experimental data for the validation of the computer codes for the prediction of two-dimensional buoyant cavity flows, Proc. ASME Meeting, HTD, Vol. 60, pp. 75-81.
- S.K. Choi, E.K. Kim and S.O. Kim [2003] Evaluation of two different k-epsilon-vv-f turbulence models for natural convection in a rectangular cavity